

# Efficient Algorithms for Private-Public Social Networks

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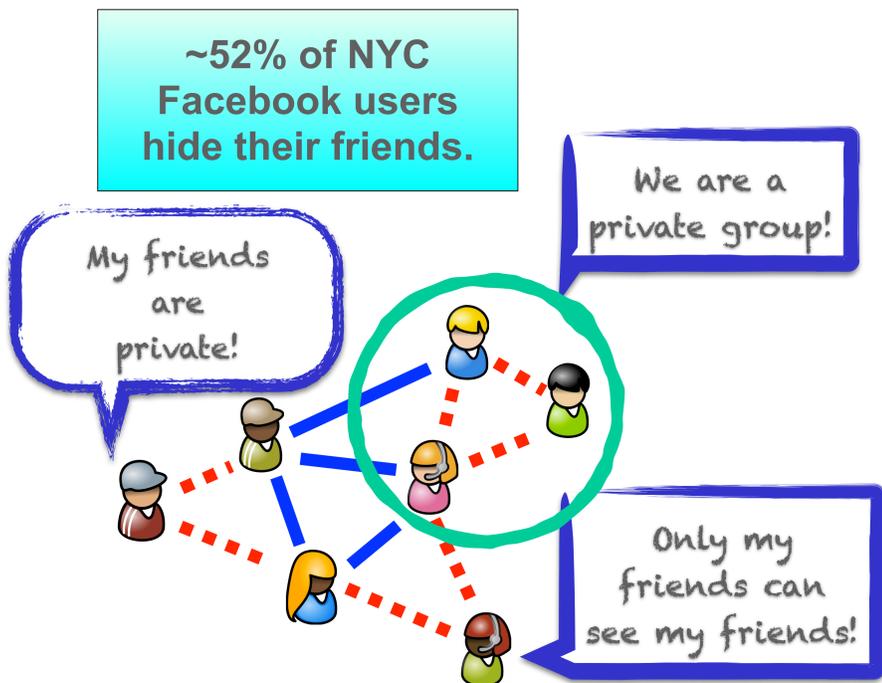
## MOTIVATION

- **Privacy** issues are a fundamental factor in the design, analysis and operation of online social networks.
- Users can specify some of their **contacts** as **private**, they can form **private groups**, etc.
- As a result, there is **not a unique social network**, but instead **each user has her own view of the network**.

The **algorithms** need to **respect** the **privacy** of the users by providing results, to a given user, based **only** on the data that user can access.

**Naive solutions:**

1. Use **only** on completely **public** data (**ineffective!**);
2. **Run** the algorithm **once** for **each** user on a **different** graph (**infeasible!**).



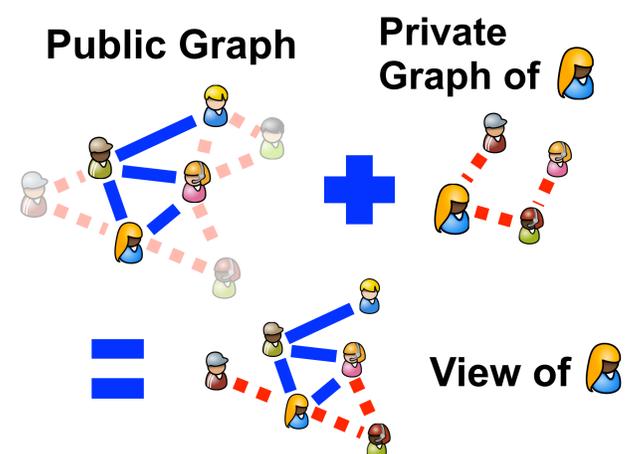
## THE PRIVATE-PUBLIC GRAPH MODEL

We introduce the **Private-Public Graph Model** which allows to design **efficient** and **effective** algorithms for several **graph problems** while **respecting** the **privacy** of every user.

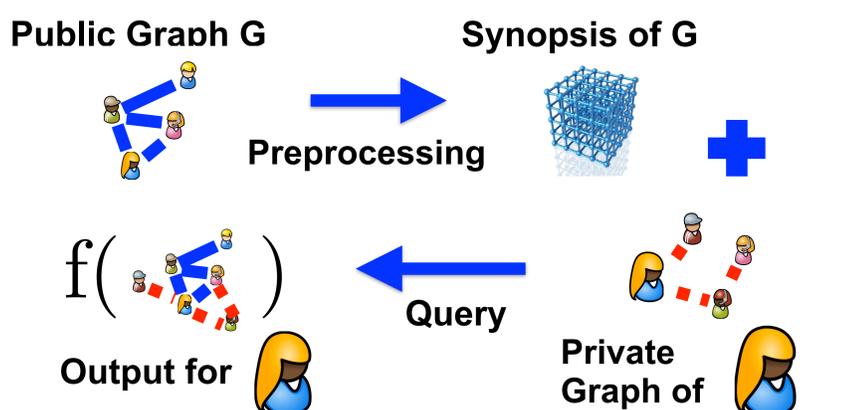
### Model

- There is a **public graph**  $G$ , visible to everyone.
- For each user  $u$  we have a **private graph**  $G_u$  visible to the user.
- We want to compute a function  $f(G+G_u)$  over the union of the public and private graphs **for each user**  $u$ .

**Assumption:**  $G_u$  edges can be up to 2-hops from  $u$  (consistent with FB, G+, etc. privacy settings).



## ALGORITHMS



Ideally, about  $O(E(G))$  preprocessing time;  $O(V(G))$  space and  $O(E(G_u))$  query time.

## EXPERIMENTS

Graph	A/B	Cosine	$\tau@50$
DBLP	6.5e-3	99.8%	88.5%
LIVEJOURNAL	3.5e-4	99.1%	69.3%
ORKUT	1.6e-3	99.9%	54.6%
YOUTUBE	1.7e-2	99.8%	80.9%

**PPR**  
**Approx.**

Up to **4 orders of magnitude faster** than the naive approach, with high accuracy.

We address several problems in this model including: **Reachability, Correlation Clustering, Personalized PageRank (PPR), Affinity Scores, etc.** using **sampling** and **sketching** techniques while providing provable guarantees.

**Numerous interesting graph problems remain open in the private-public model.**