



SAPIENZA  
UNIVERSITÀ DI ROMA

# Spreading Rumours without the Network

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# Rumour Spreading

Diffusive processes on graphs are an important paradigm in several fields:

- **Systems:** How to spread information on network?
- **Social Networks:** Why posts become viral?
- **Sociology:** What makes innovations/products accepted?
- **Epidemiology:** How diseases spread?

We consider various models of information diffusion: **Push**, **Pull** and **SIR**.



# Background

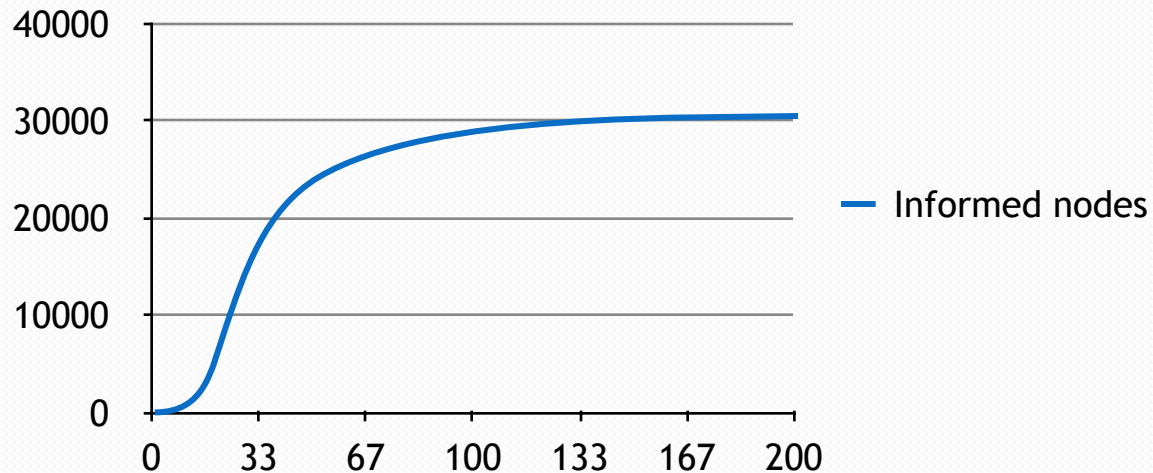
Most results known are asymptotic bounds on the competition time:

- At most  $O(n \log(n))$  (Feige et. al, 90)
- Fast in Erdos Reyni and Preferential Attachment (Elsasser et al. 2006, Chierichetti et al. 2009).
- Fast in high conductance graphs. (Chierichetti et al. 2010, Giakkoupis et al. 2011)

# Our Goal

## Goal #1: Beyond asymptotics

We are interested in the expected number of informed nodes for each time step of the process

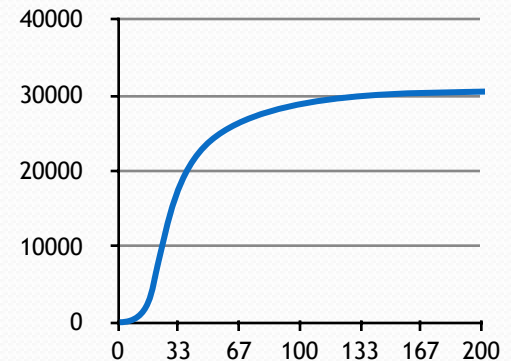
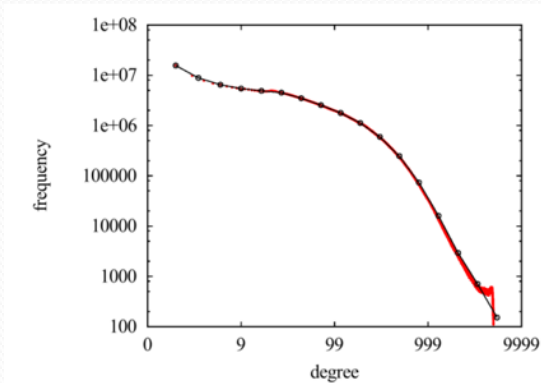


**Notice:** this is known only for very simple graphs (e.g. Clique, Pittel '87)

# Our Goal

## Goal #2: Prediction with limited information

**Motivation:** real networks are often unavailable

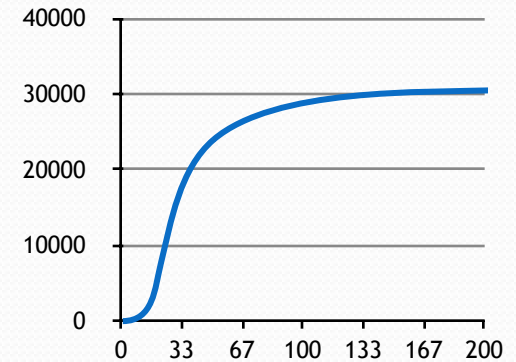
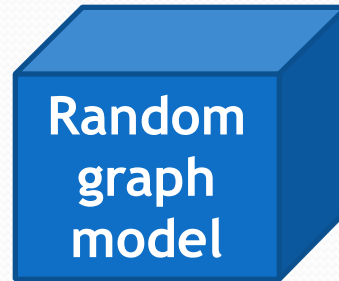
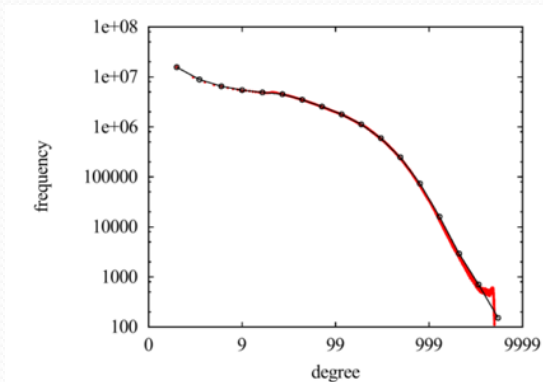


**Caveat:** this is clearly an ill-posed question...

... But surprisingly, it is possible for real social network

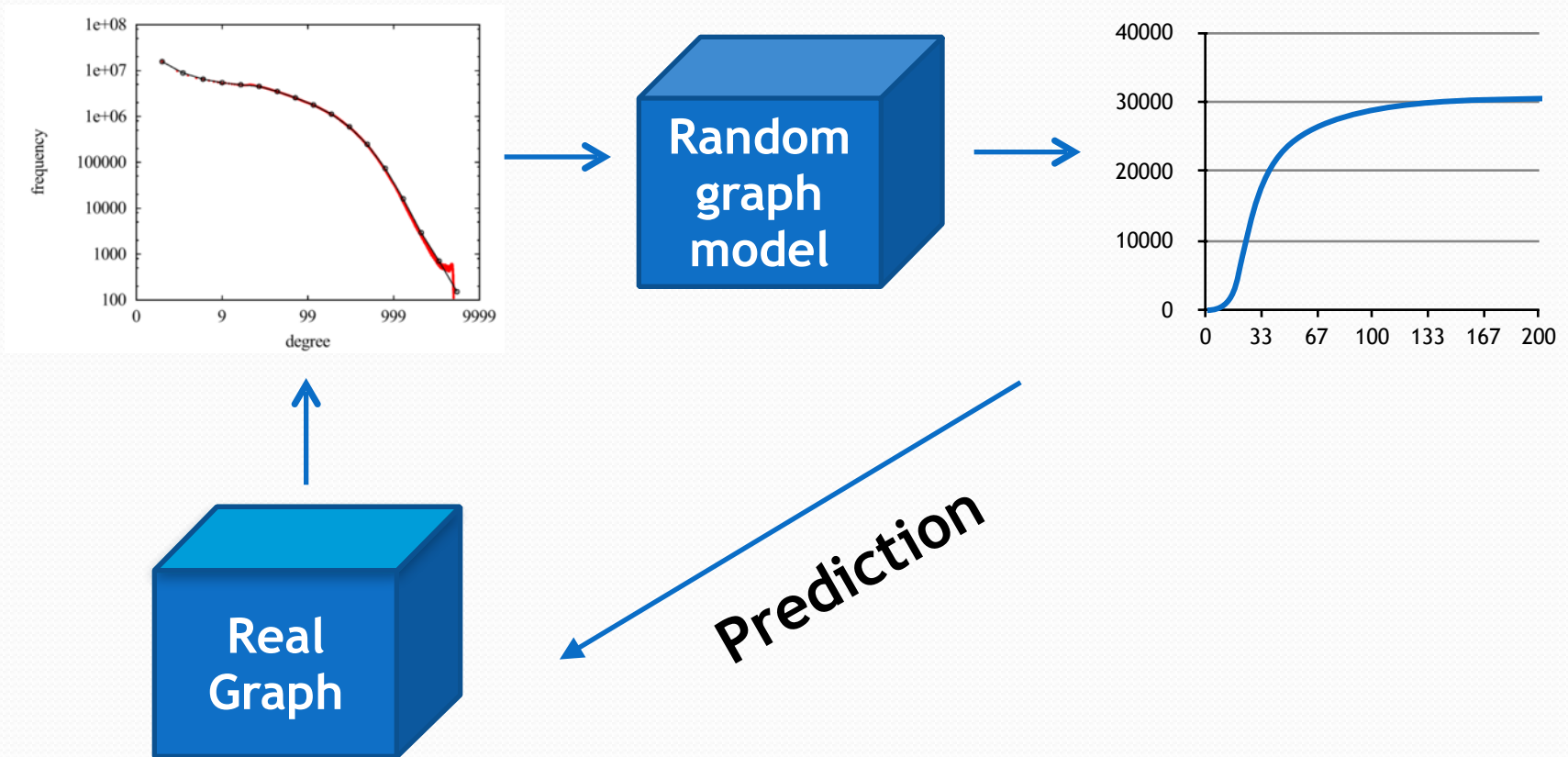
# How Can we Achieve this?

A simpler problem: model the *unknown graph* by a *known random* graph generation process.



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# Which Graph Model?

We use the **configuration model** as random graph model.

SIR on configuration model matches real post diffusions in **Twitter** (Goel et al., 2013):

- Distribution of **popularity** of posts.
- **Virality** of the diffusion.



# Our Contribution

A predictor algorithm for the **configuration model** for the **Push, Pull** and **SIR** Processes:

- Space efficient: very large graphs can fit in memory.
- Provably exact on random graphs.

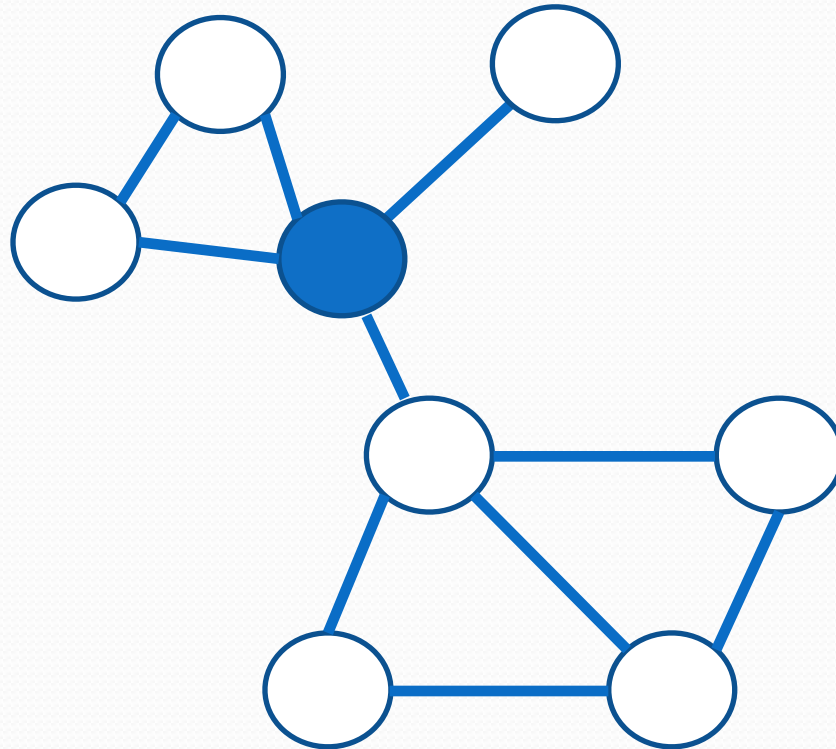
**The algorithm predicts accurately the both the popularity and the virality on real social networks.**

# Outline of the Talk

- The diffusion processes;
- Our algorithm(s);
- Experimental evaluation;
- Conclusions.

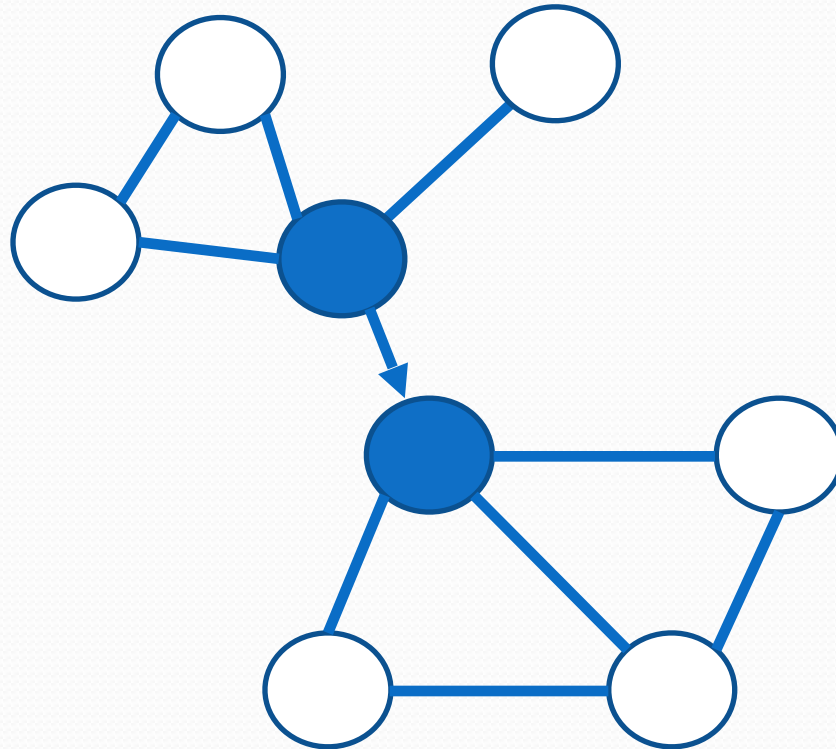
# The Push-Pull Process

# Push-Pull Protocol



**PUSH**

# Push-Pull Protocol

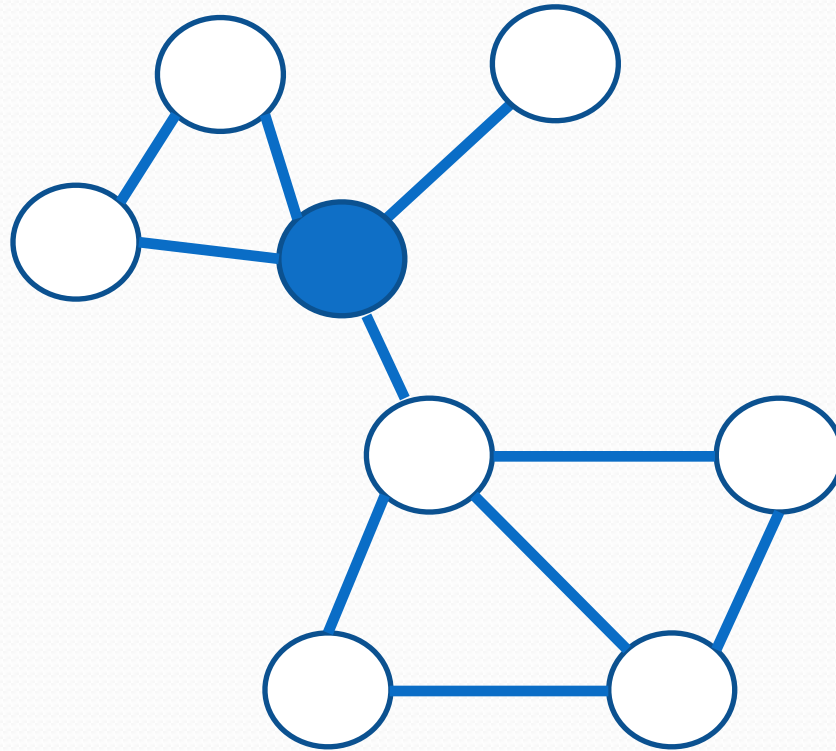


**PUSH**





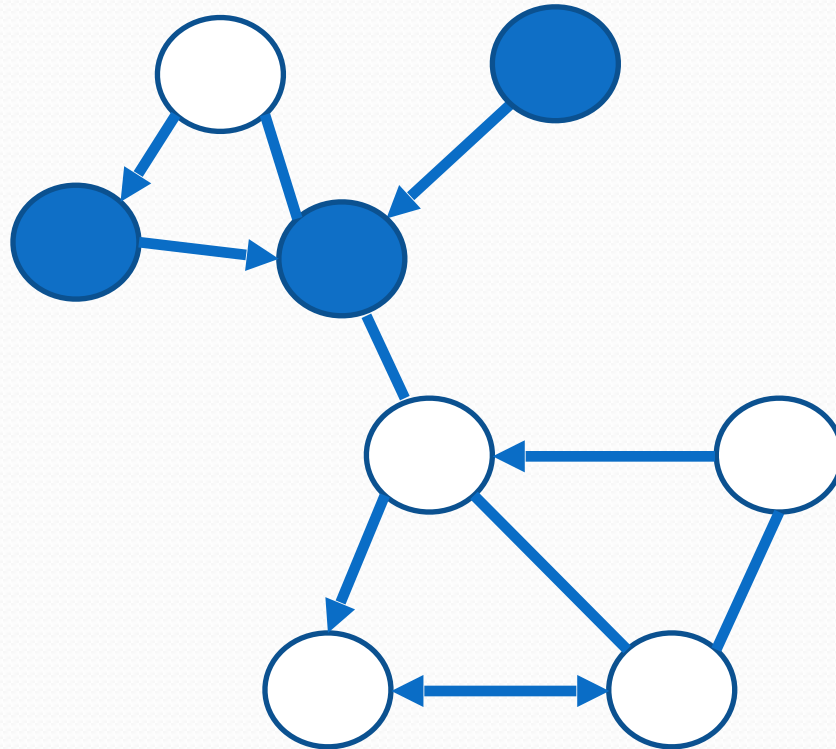
# Push-Pull Protocol



**PULL**

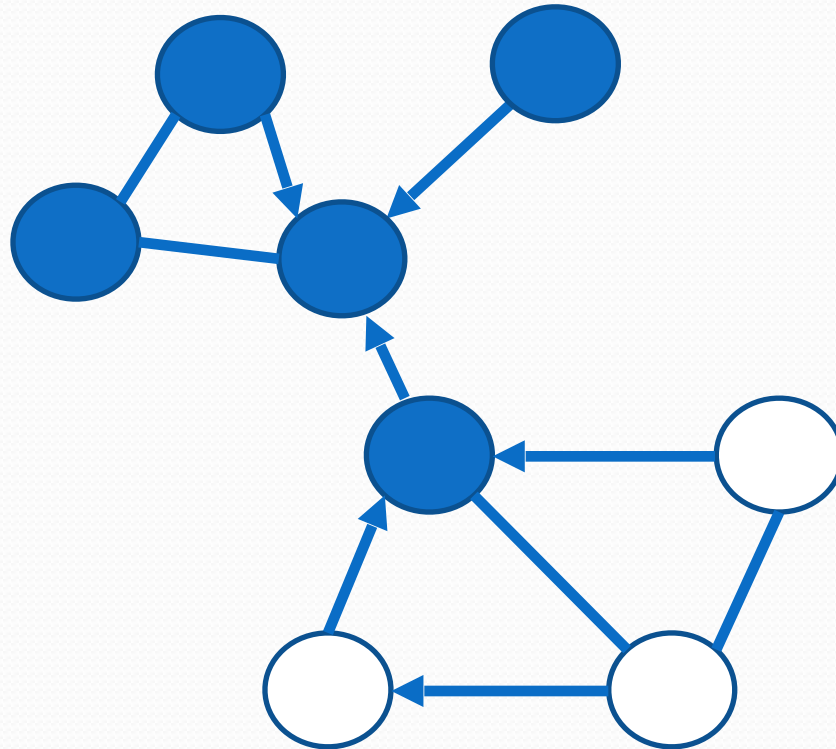


# Push-Pull Protocol



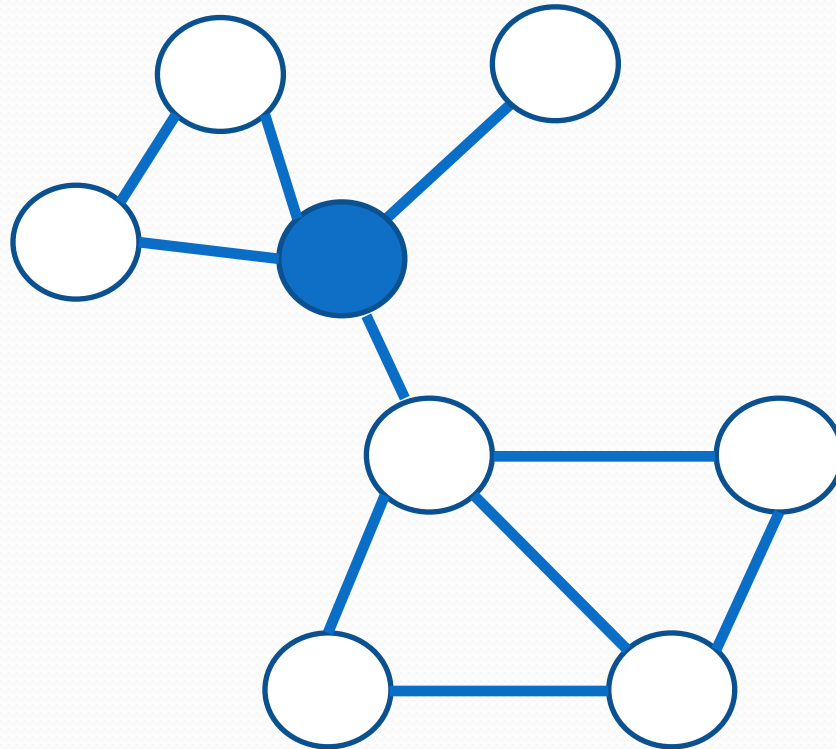
**PULL**

# Push-Pull Protocol



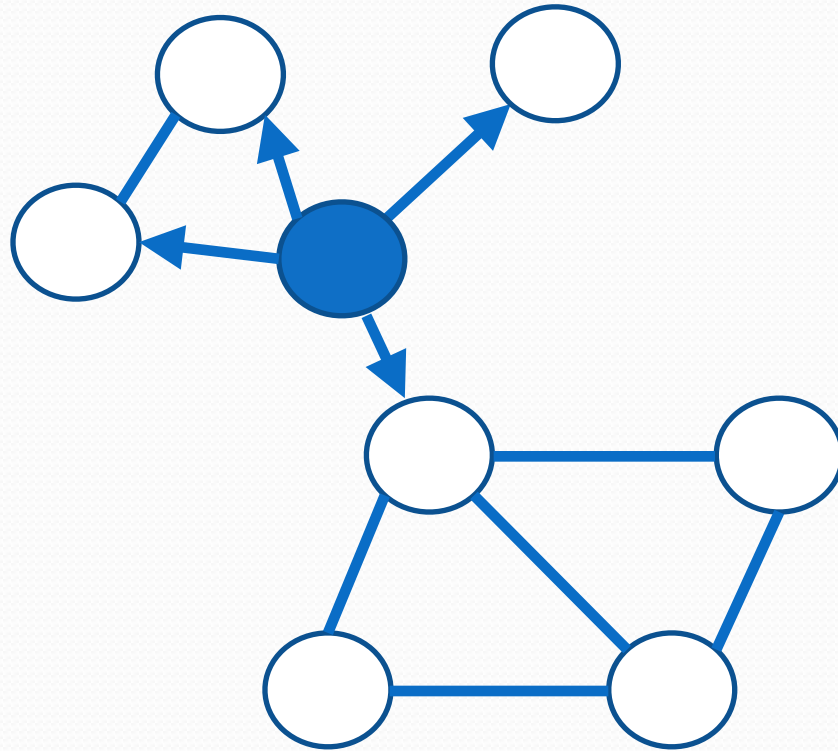
**PULL**

# SIR Process



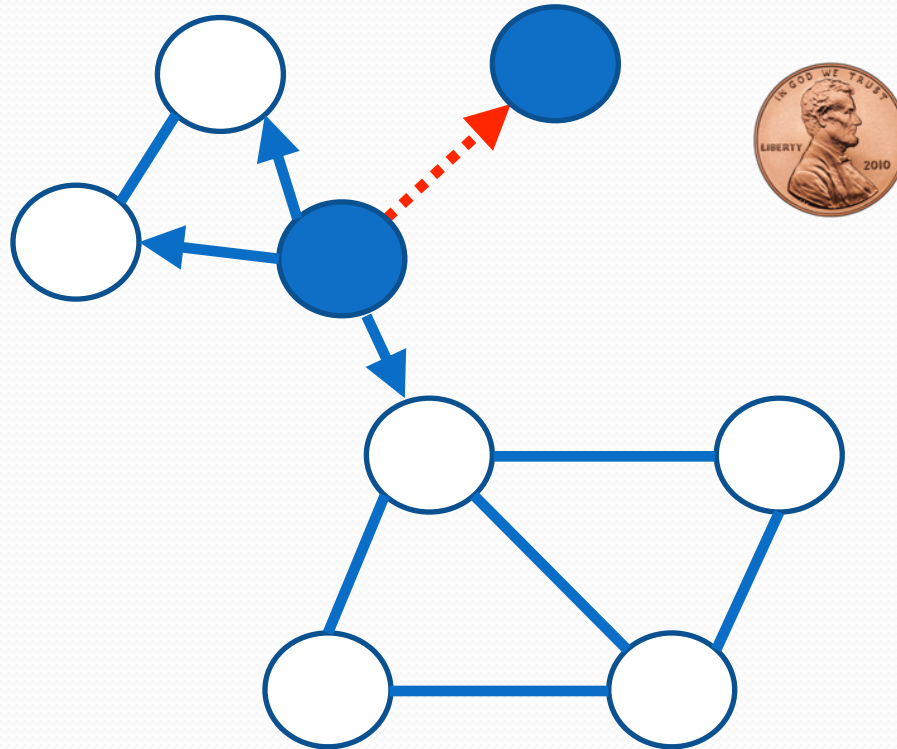
**SIR**

# SIR Process



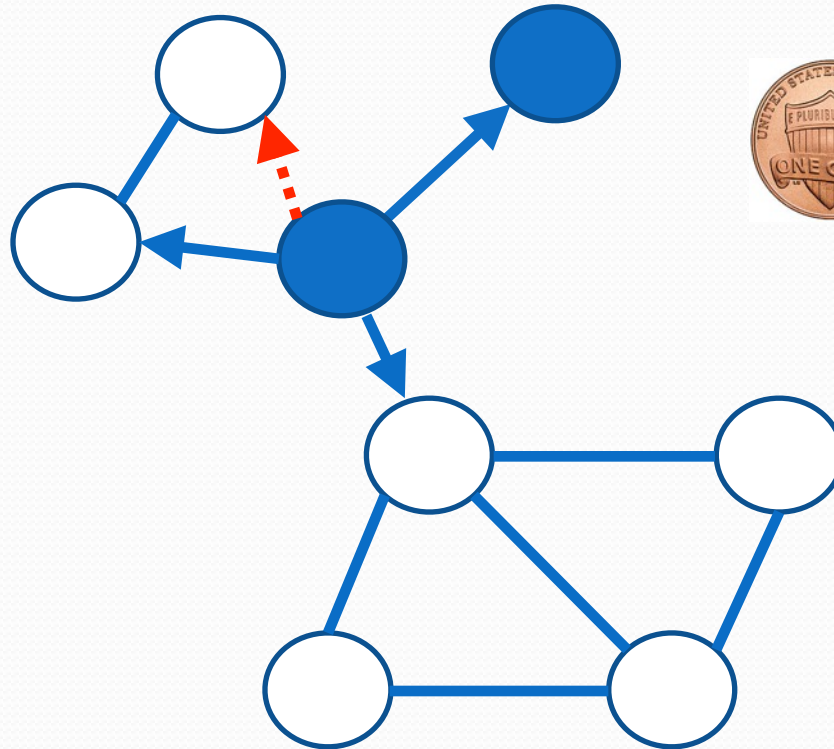
**SIR**

# SIR Process



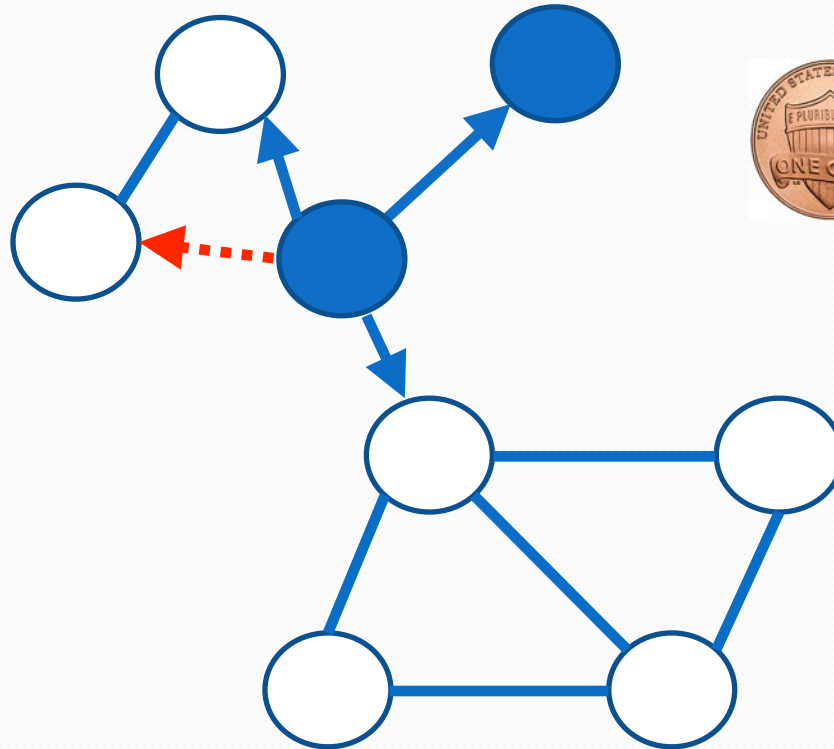
**SIR**

# SIR Process



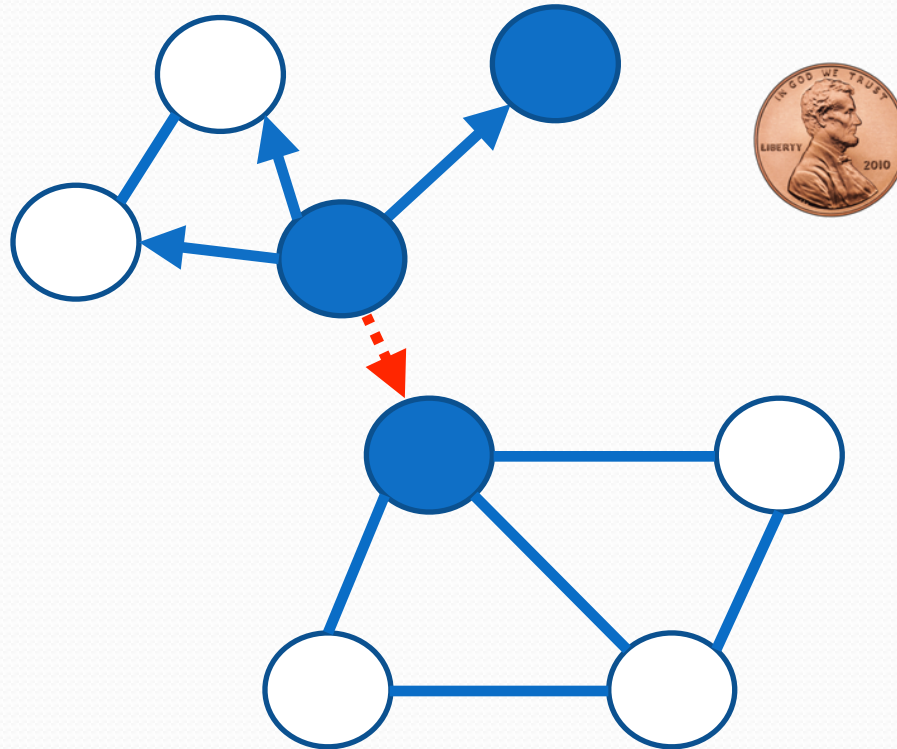
**SIR**

# SIR Process



**SIR**

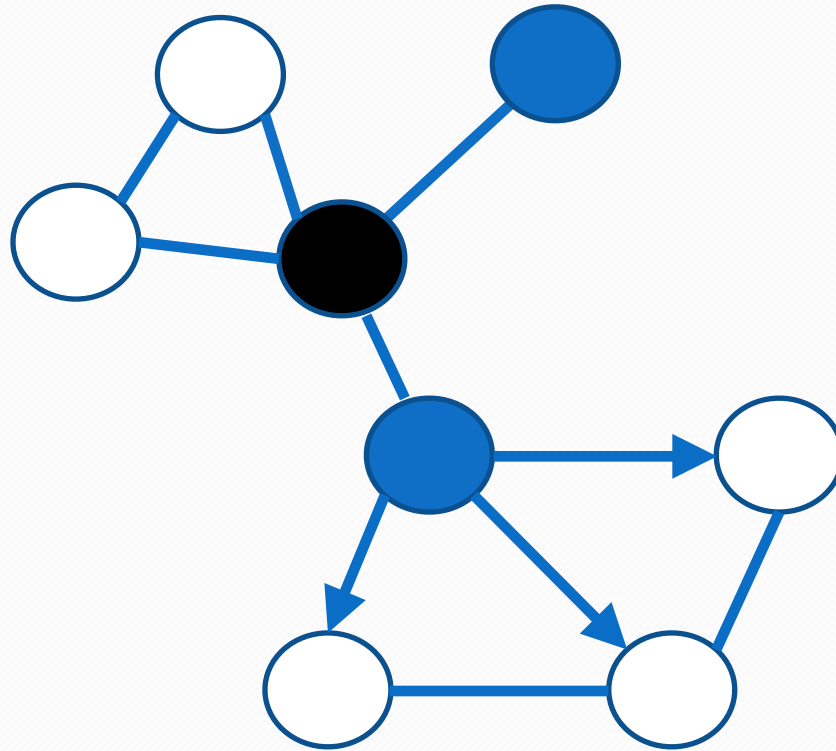
# SIR Process



**SIR**



# SIR Process



**SIR**

# Our Algorithm

# Naive Solution

**Simulate two random processes:** the network generation and the rumour spreading.

**Naive algorithm:**

- Generate a random network  $G$ .
- Simulate rumour spreading on  $G$ .
- Run several times **in parallel** and average.

**Space bottleneck:** Real networks are too large to fit in main memory!

# Our Approach

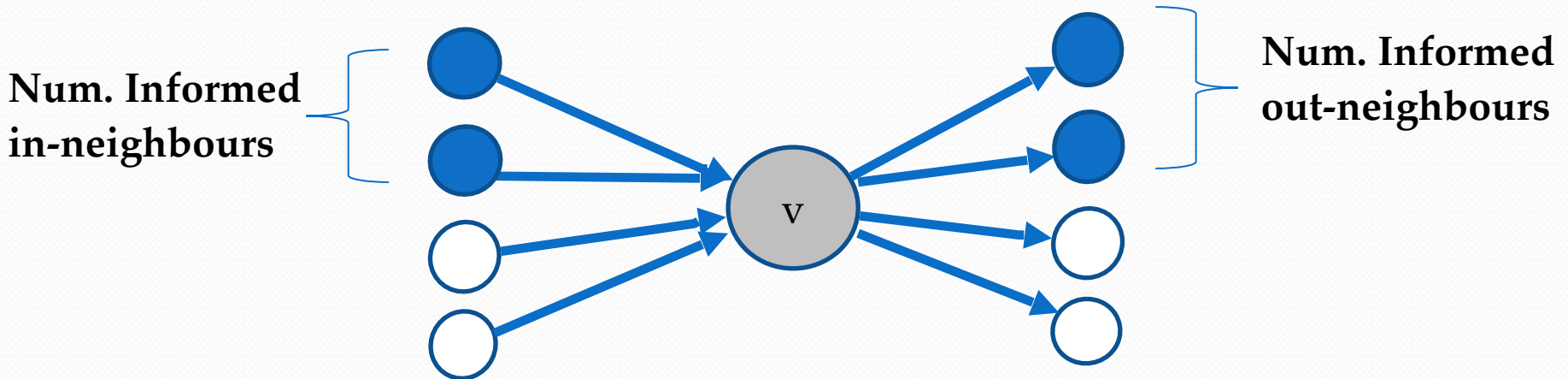
We can reduce the space to  $O(n)$  vs  $O(n+m)$  in directed graphs and even  $o(n)$  in undirected ones.

This is a significant reduction not only in asymptotic!

**Deferred decision principle:** the topology is *discovered* as nodes are involved in the rumor spreading process and immediately *forget*.

# Intuition

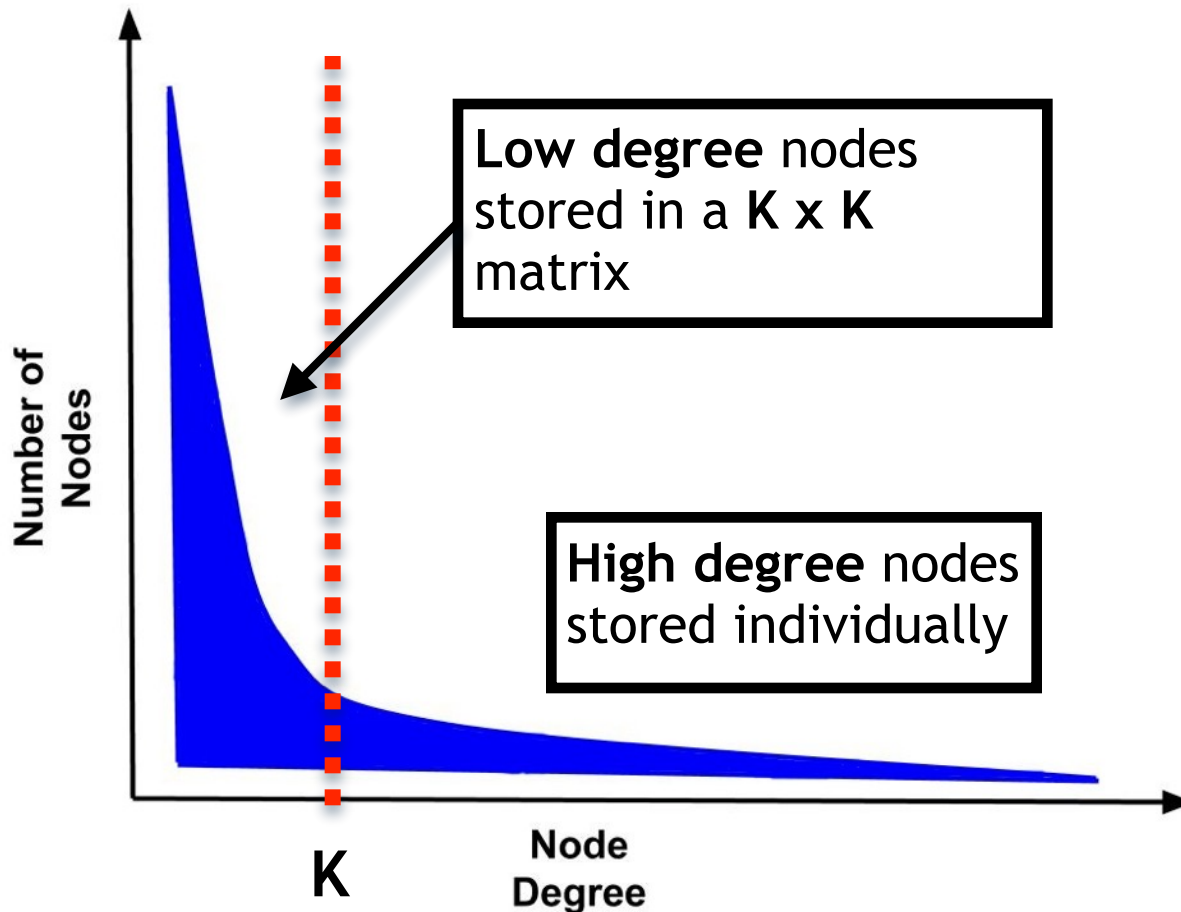
Only the local neighbourhood determines the evolution of the process.



We do not store the edges of the graph.

# Undirected Graphs

We use an efficient matrix representation.



# Undirected Graphs

Graph	Nodes	Matrix Size	Saving in space
<i>Livejournal</i>	<i>5M</i>	<i>176</i>	<i>98%</i>
<i>Facebook (estimates)</i>	<i>720M</i>	<i>&lt;5000</i>	<i>&gt;97%</i>

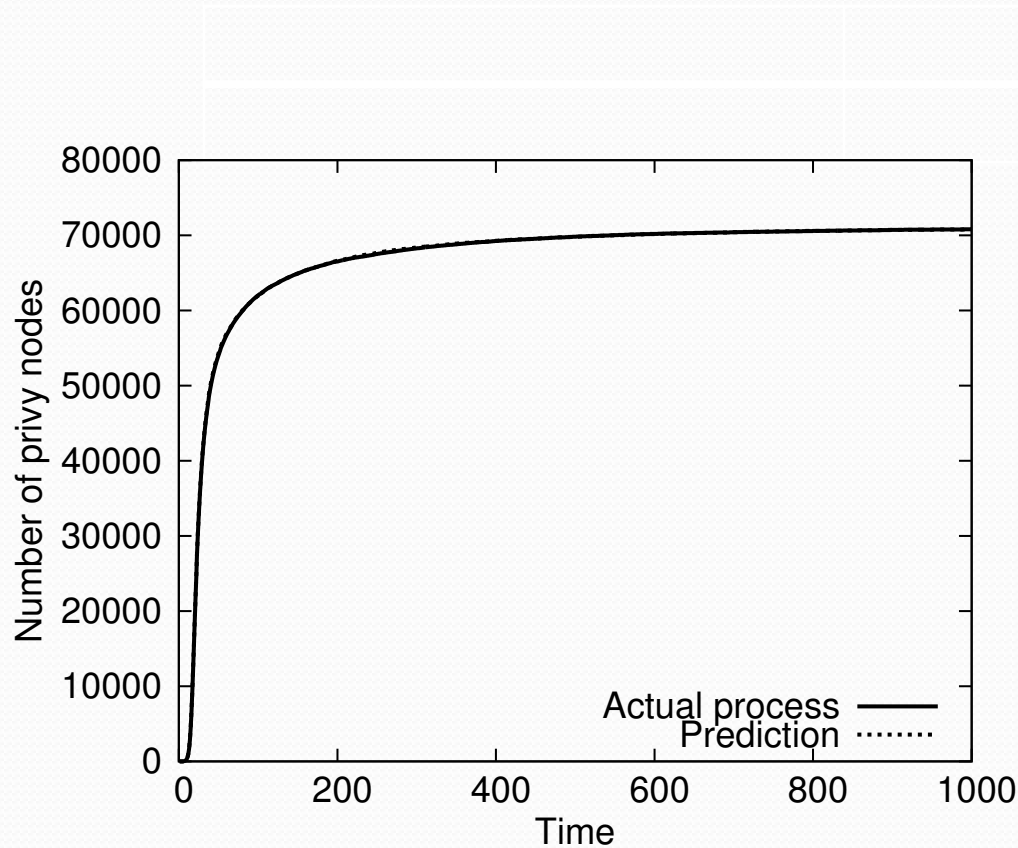
For power law graphs of exponent  $\alpha$  the cost is  $n^{\frac{2}{1+\alpha}}$

In practice the entire Facebook graph could fit in few gigabytes.

# Results on Random Graphs



# Results on Random Graphs

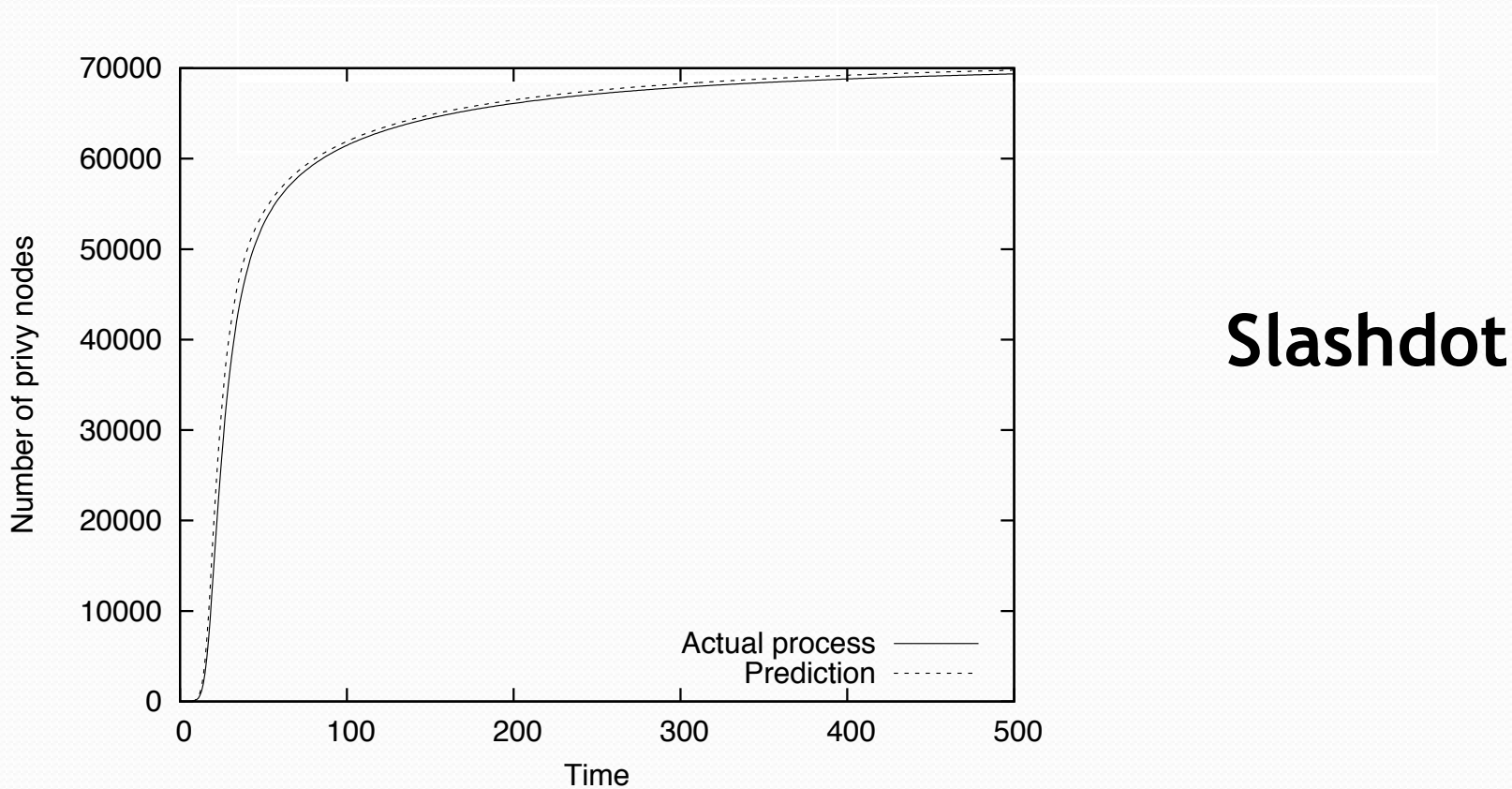


The model prediction  
is perfect

This can be proved formally.

# Results on Real Graphs

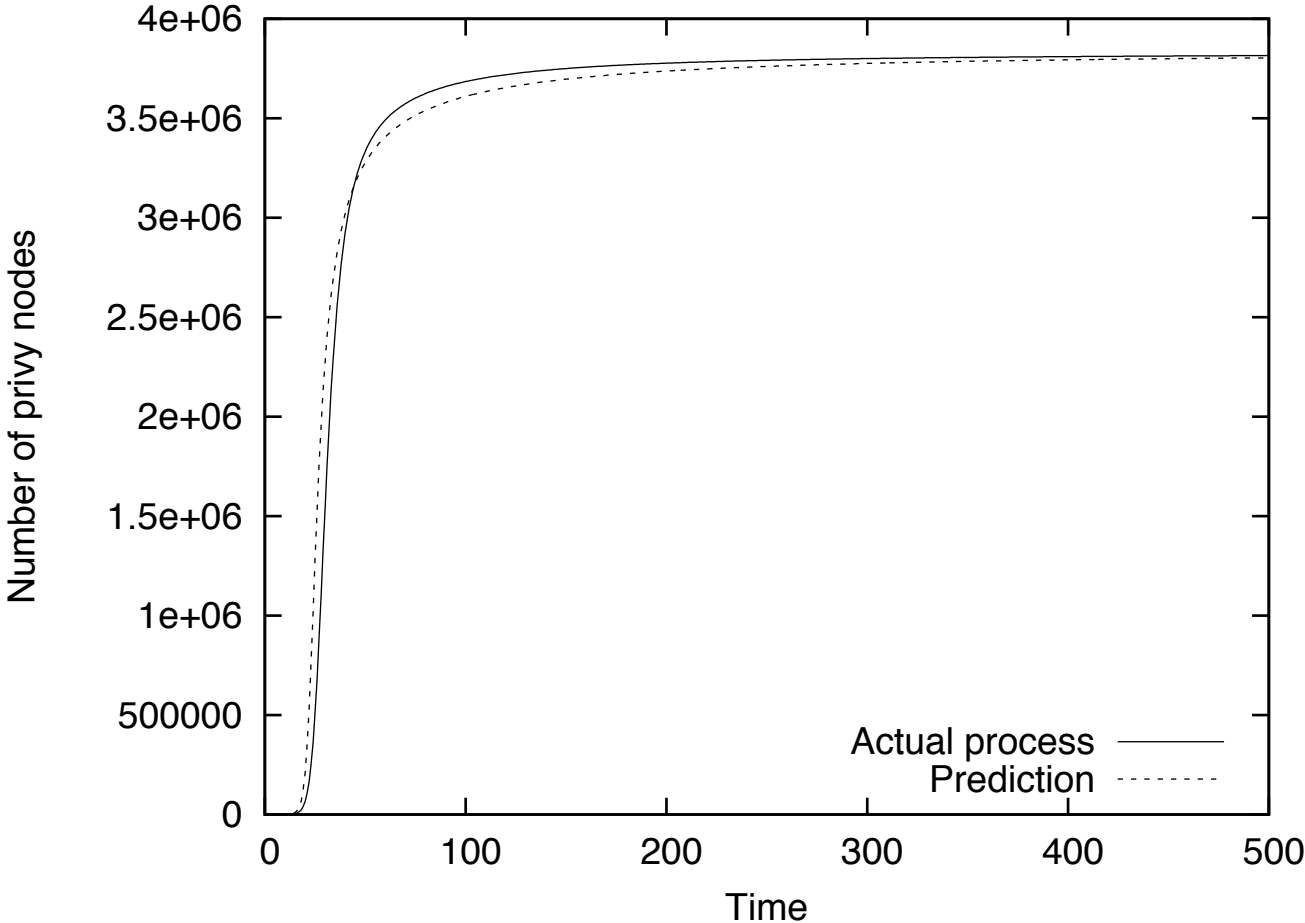
# Social Networks - Push



**Slashdot**

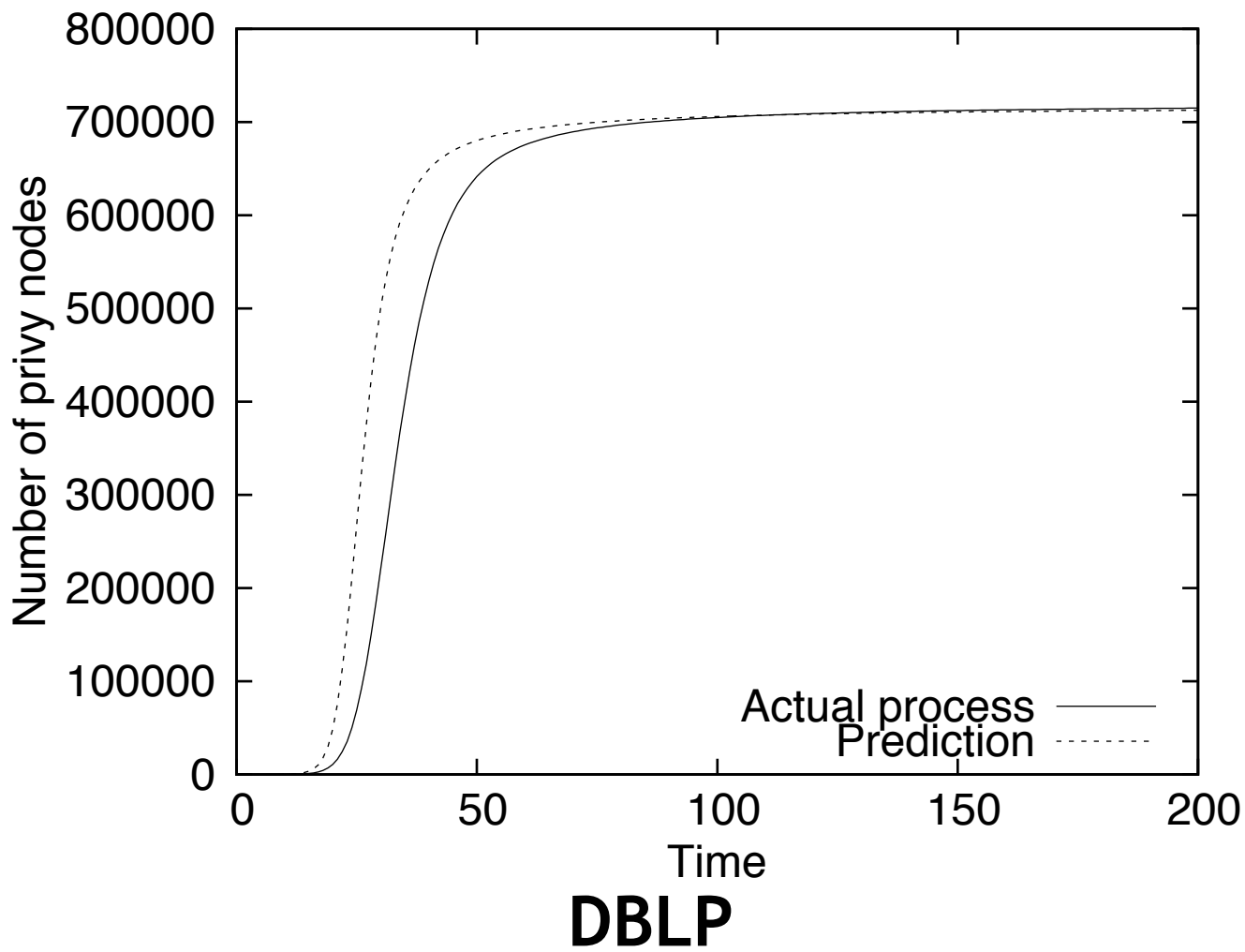
**The model is qualitatively accurate for the social network we tested**

# More Social Networks - Push

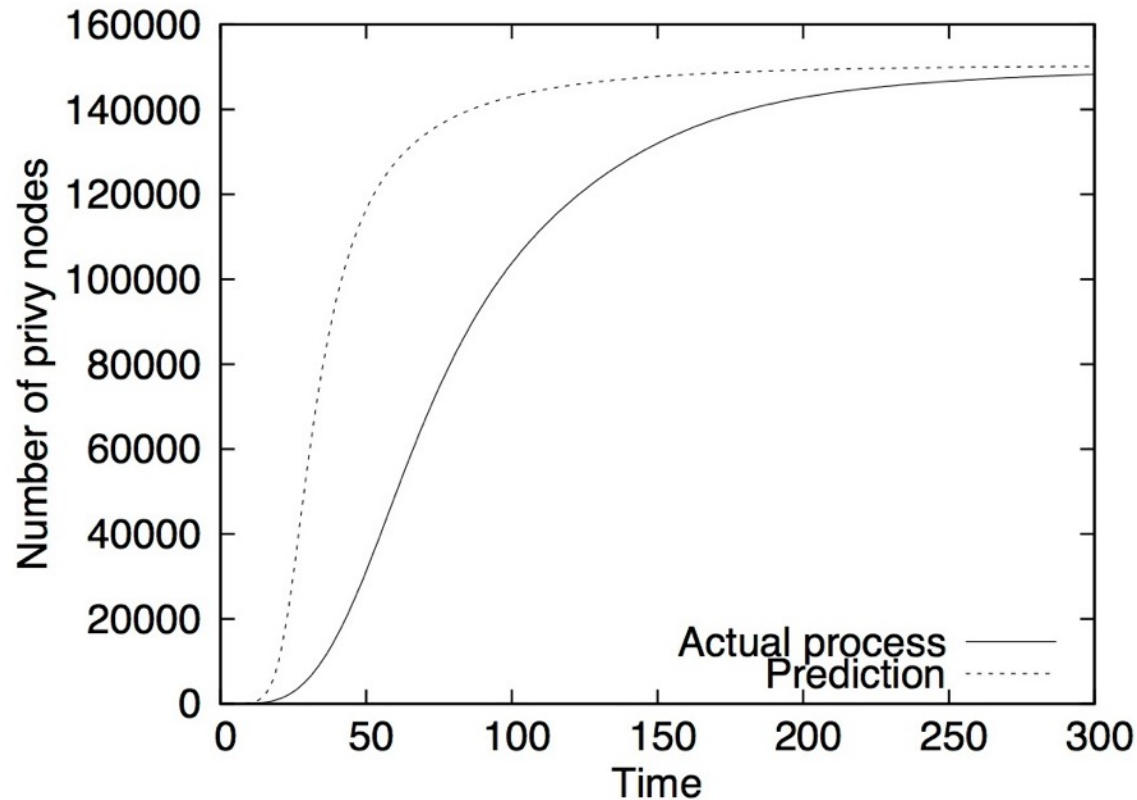


Livejournal

# More Social Networks - Push



# Non-Social Networks - Push



Web Stanford

**For non-social networks the prediction is not accurate.**

# Results

Prediction performances strongly depends on the network class:

- Very good for **social networks**: friendship graphs, trust networks, collaboration networks.
- Poor for **non-social networks**: web graphs, road networks, etc.

This dichotomy has been observed in other contexts: degree correlations, graph compressibility, etc.

**What is the reason for this phenomenon?**

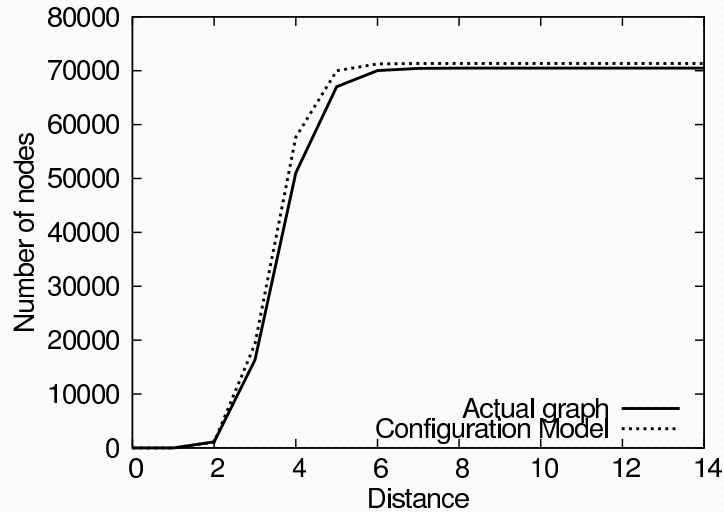
# Neighbourhood Function

The neighbourhood function  $F(t)$  of graph measures how many pairs of nodes are at distance  $\leq t$

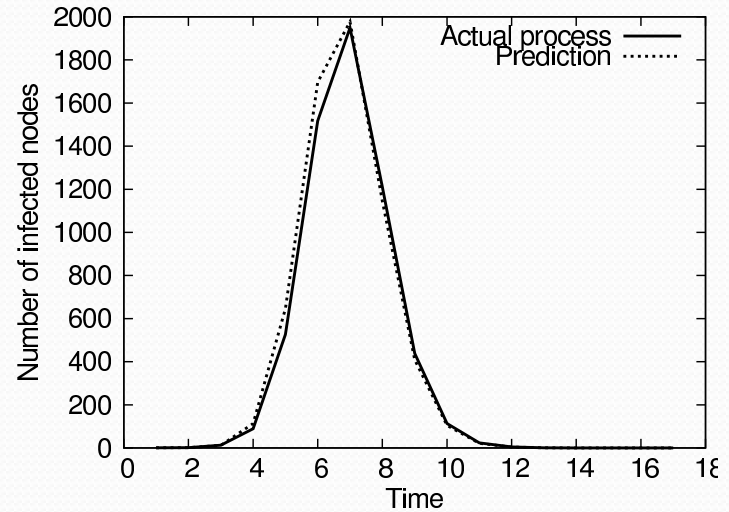
This measure has been shown to tell apart social and non-social graphs.



# Neighbourhood F. vs Prediction Quality



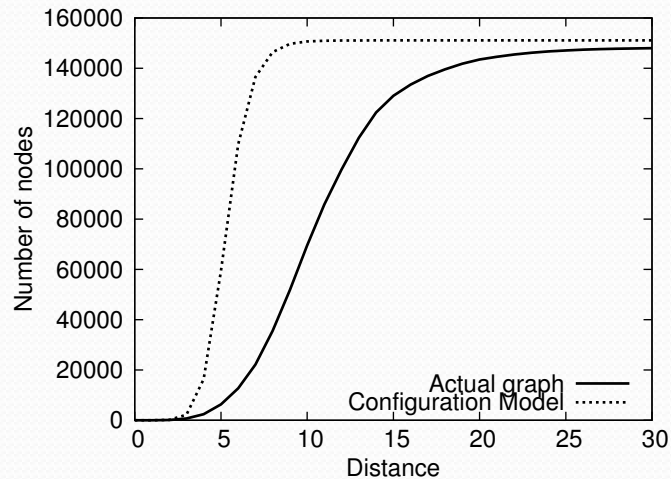
Slashdot Neighbourhood F.



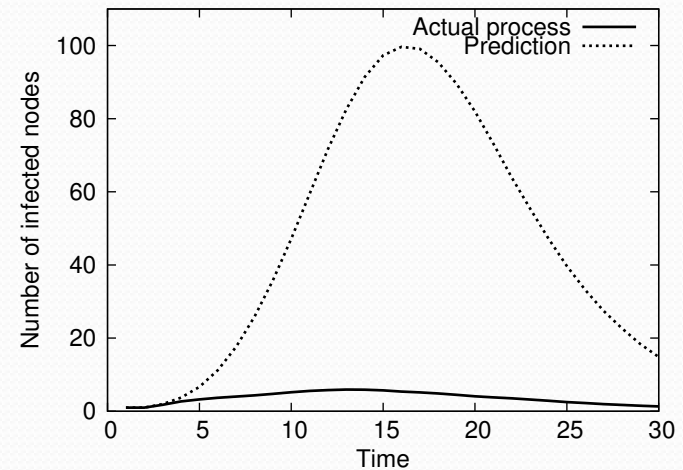
Slashdot Prediction - SIR

**Social graphs have a neighbourhood function close to the configuration model.**

# Neighbourhood F. vs Prediction Quality



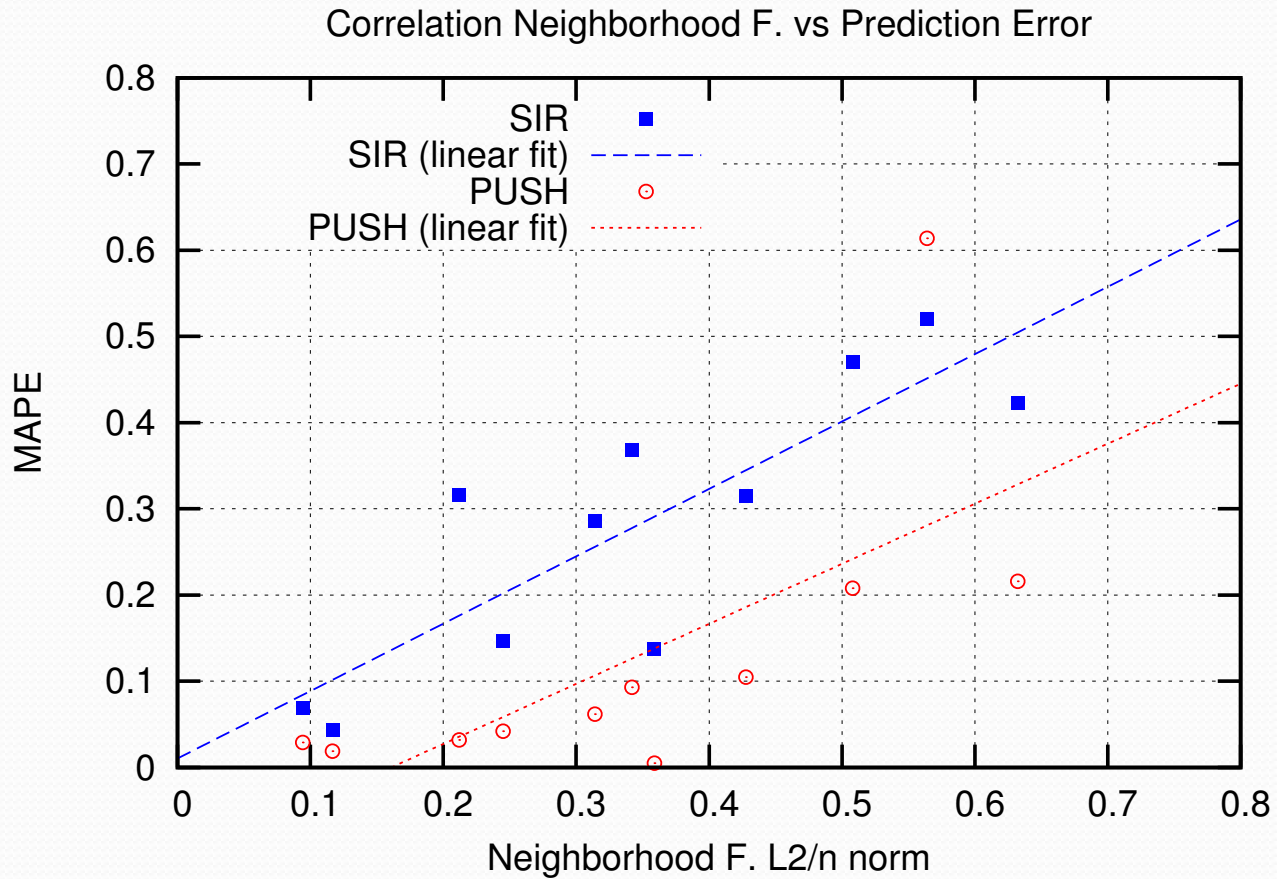
Web Graph Neighbourhood F.



Web Graph Prediction - SIR

**Non-Social graphs have a neighbourhood function far from the configuration model.**

# Neighbourhood F. vs Prediction Quality



The correlation is strong and statistically significant.

# Conclusion

- Rumour spreading processes can be predicted accurately in social graphs based on very limited information on the graph.
- Our predictor is provably correct and space efficient.
- We characterise the class of graph that can be predicted based on the Neighbourhood Function.
- We would like to extend our model to more nuanced diffusion processes.

**Thank you for your attention!**